

CLAIMS

1. Method of generating electronic keys d for a public-key cryptography method using an electronic device, mainly characterized in that it comprises two separate calculation steps:

Step A

1) calculating pairs of prime numbers (p, q) or values representative of pairs of prime numbers, this calculation being independent of knowledge of the pair (e, l) in which e is the public exponent and l is the length of the key of the cryptography method, l also being the length of the modulus N of said method,

15 2) storing the pairs or values thus obtained;

Step B

20 calculating a key d from the results of step A and knowledge of the pair (e, l) .

2. Method of generating electronic keys according to Claim 1, characterized in that step A-1) consists in calculating pairs of prime numbers (p, q) 25 without knowledge of the public exponent e or of the length l of the key, using a parameter Π which is the product of small prime numbers, so that each pair (p, q) has a maximum probability of being able to correspond to a future pair (e, l) and can make it possible to 30 calculate a key d .

3. Method of generating electronic keys according to Claim 2, characterized in that the calculation of step A-1) also takes account of the fact

that e has a high probability of forming part of the set $\{3, 17, \dots, 2^{16+1}\}$, and for this use is made in the calculation of a seed σ which makes it possible to calculate not pairs (p, q) but a representative value
5 referred to as the image of the pairs (p, q) .

4. Method of generating electronic keys according to Claims 1 and 3, characterized in that the storage A-2) consists in storing the image of the
10 pairs.

5. Method of generating electronic keys according to Claim 1, characterized in that step A-1) consists in calculating pairs of prime numbers (p, q)
15 for different probable pairs (e, l) .

6. Method of generating electronic keys according to Claims 2 and 5, characterized in that the parameter Π contains the usual values of the public
20 exponent e , for example 3, 17.

7. Method of generating electronic keys according to Claim 1, characterized in that step A-1) comprises an operation of compressing the calculated
25 pairs (p, q) and step A-2) then consists in storing the compressed values thus obtained.

8. Method of generating electronic keys according to Claim 1, characterized in that step A-1) comprises the generation of a prime number q for which
30 a lower limit B_0 is set for the length l_0 of this prime number that is to be generated, such that $l_0 \geq B_0$, for example $B_0 = 256$ bits, and in that it comprises the following sub-steps:

1) calculating parameters v and w from the following relations and storing them:

$$v = \sqrt{2^{2\ell_0-1}/\Pi}$$

$$w = 2^{\ell_0}/\Pi$$

5 in which Π is stored and corresponds to the product of the f smallest prime numbers, f being selected such that $\Pi \leq 2^B$,

2) selecting a number j within the range of integers $\{v, \dots, w-1\}$ and calculating $\ell=j \mod \Pi$;

10 3) selecting and storing a prime number k of short length compared to the length of an RSA key within the range of integers $\{0, \dots, \Pi-1\}$, (k, Π) being co-prime;

$$4) \text{ calculating } q=k+\ell,$$

15 5) verifying that q is a prime number, if q is not a prime number then:

a) taking a new value for k using the following relation:

20 $k = a \cdot k \pmod{\Pi}$; a belonging to the multiplicative group Z_{Π}^* of integers modulo Π ;

b) repeating the method from step 4).

25 9. Method of generating electronic keys according to Claims 3 and 8, characterized in that the numbers j and k can be generated from the seed σ stored in memory.

30 10. Method of generating electronic keys according to Claim 8, characterized in that the prime number p is generated by repeating all the above sub-steps while replacing q with p and replacing ℓ_0 with $\ell-\ell_0$.

11. Method of generating electronic keys according to any one of the preceding claims, characterized in that:

5 step B comprises, for a pair (p, q) obtained in step A:

- verifying the following conditions:

(i) $p-1$ and $q-1$ are prime numbers with a given e and

(ii) $N=p \cdot q$ is an integer of given length l ,

10 - if the pair (p, q) does not satisfy these conditions:

- selecting another pair and repeating the verification until a pair is suitable,

15 - calculating the key d from the pair (p, q) obtained.

12. Secure portable object able to generate electronic keys d of an RSA-type cryptography algorithm, characterized in that it comprises at least:

20 - communication means for receiving at least one pair (e, l) ,

- a memory for storing the results of a step A consisting in:

25 calculating pairs of prime numbers (p, q) or values representative of pairs of prime numbers, this calculation being independent of knowledge of the pair (e, l) in which e is the public exponent and l is the length of the key of the cryptography method, l also being the length of the modulus N of this p ,

30 - a program for implementing a step B consisting in:

calculating a key d from the results of step A and knowledge of a pair (e, l) .

13. Secure portable object according to Claim 12, characterized in that it also comprises a program for implementing step A, steps A and B being separate in
5 terms of time.

14. Secure portable object according to Claim 13, characterized in that the program for implementing step A carries out the following sub-steps:

10 1) calculating parameters v and w from the following relations and storing them:

$$v = \sqrt{2^{2\ell_0-1}/\Pi}$$

$$w = 2^{\ell_0}/\Pi$$

15 in which Π is stored and corresponds to the product of the f smallest prime numbers, f being selected such that $\Pi \leq 2^{B_0}$, B_0 is a lower limit set for the length ℓ_0 of the prime number that is to be generated, such that $\ell_0 \geq B_0$, for example $B_0 = 256$ bits

20 2) selecting a number j within the range of integers {v, ..., w-1} and calculating $\ell=j \mod \Pi$;

3) selecting and storing a prime number k of short length compared to the length of an RSA key within the range of integers {0, ..., $\Pi-1$ }, (k, Π) being co-prime;

25 4) calculating $q=k+\ell$,

5) verifying that q is a prime number, if q is not a prime number then:

a) taking a new value for k using the following relation:

30 $k = a \cdot k \pmod{\Pi}$; a belonging to the multiplicative group \mathbb{Z}_{Π}^* of integers modulo Π ;

b) repeating the method from step 4).

15. Secure portable object according to Claim 12 or 13 or 14, characterized in that it consists of a chip card.